



Tutorials and worked examples for simulation,  
curve fitting, statistical analysis, and plotting.  
<http://www.simfit.org.uk>

When the 2-way ANOVA assumptions are not justified, the Friedman nonparametric 2-way analysis of variance by ranks is often used. This investigates the score differences between  $k$  matched sets of size  $l$ . If  $k = 2$  then the sign test, or else the Wilcoxon signed rank test, should be used.

From the main SIMFIT menu choose [Statistics], [ANOVA], then the Friedman test, and read in data from the default test file `anova2.tf1`, which has data for scores for matched samples of eighteen rats under three different patterns of enforcement as follows.

```

1.00  3.00  2.00
2.00  3.00  1.00
1.00  3.00  2.00
1.00  2.00  3.00
3.00  1.00  2.00
2.00  3.00  1.00
3.00  2.00  1.00
1.00  3.00  2.00
3.00  1.00  2.00
3.00  1.00  2.00
2.00  3.00  1.00
2.00  3.00  1.00
3.00  2.00  1.00
2.00  3.00  1.00
2.50  2.50  1.00
3.00  2.00  1.00
3.00  2.00  1.00
2.00  3.00  1.00

```

Analysis then leads to the results below.

Friedman Nonparametric 2-way ANOVA	
Test Statistic ( $FR$ )	8.583
Number of degrees of freedom	2
Significance (i.e., p-value)	0.0137

As the data matrix represents scores rather than normally distributed variables with identical variances, the matrix was analyzed as a two way table with  $k = 18$  rows, and  $l = 3$  columns, using the nonparametric Friedman 2-way ANOVA procedure to test

$H_0$  : all medians are equal, against the alternative,

$H_1$  : they come from different populations.

The procedure ranks column scores as  $r_{ij}$  for row  $i$  and column  $j$ , assigning average ranks for ties, works out rank sums as  $t_i = \sum_{j=1}^l r_{ij}$ , then calculates  $FR$  given by

$$FR = \frac{12}{kl(k+1)} \sum_{i=1}^k (t_i - l(k+1)/2)^2.$$

For small samples, exact significance levels are calculated, while for large samples it is assumed that  $FR$  follows a  $\chi_{k-1}^2$  distribution.